

SENIOR DIVISION SOLUTIONS

<p>1. Prefix/Infix/Postfix Notation</p> $ \begin{aligned} &ABC + *BC * / A 2 \uparrow C - BC - / + \\ &= A (BC +) *(BC *) / (A 2 \uparrow) C - (BC -) / + \\ &= [A (+BC) *] (*BC) / [(\uparrow A 2) C -] (-BC) / + \\ &= [(* A + BC) (*BC) /] [(- \uparrow A 2 C) (-BC) /] + \\ &= [(/ * A + BC * B C) (/ - \uparrow A 2 C - B C) +] \\ &= + / * A + B C * B C / - \uparrow A 2 C - B C \end{aligned} $	1. As shown
<p>2. Prefix/Infix/Postfix Notation</p> $ \begin{aligned} /! a * ! - a b ! b &= / (! 8) * ! (- 8 6) (! 6) = / (8!) * [! 2] (6!) \\ &= / (8!) [* (2!)(6!)] = / (8!) (2! * 6!) = 8! / (2! * 6!) \\ &= 40320 / (2 * 720) = 40320 / 1440 = 28 \end{aligned} $	2. 28
<p>3. Bit-String Flicking</p> $ \begin{aligned} &(\text{LSHIFT}-2 (10110 \text{ AND } (\text{NOT } 00100))) \text{ OR} \\ &\quad (\text{RCIRC}-1 (\text{RSHIFT}-1 (11011 \text{ AND } (\text{LCIRC}-2 10001)))) \\ &= (\text{LSHIFT}-2 (10110 \text{ AND } 11011)) \text{ OR} \\ &\quad (\text{RCIRC}-1 (\text{RSHIFT}-1 (11011 \text{ AND } 00110))) \\ &= (\text{LSHIFT}-2 10010) \text{ OR } (\text{RCIRC}-1 (\text{RSHIFT}-1 00010)) \\ &= 01000 \text{ OR } (\text{RCIRC}-1 00001) = 01000 \text{ OR } 10000 = 11000 \end{aligned} $	3. 11000
<p>4. Bit-String Flicking</p> <p>Let $X = abcde$</p> $ \begin{aligned} &(\text{RSHIFT}-1 (\text{LCIRC}-2 X)) \text{ OR } (\text{NOT}(\text{RCIRC}-3(\text{LSHIFT}-1 00100))) = 11110 \\ &\text{LHS} = (\text{RSHIFT}-1 (\text{LCIRC}-2 abcde)) \text{ OR } (\text{NOT}(\text{RCIRC}-3 01000)) \\ &= (\text{RSHIFT}-1 cdeab) \text{ OR } (\text{NOT } 00001) \\ &= 0cdea \text{ OR } 11110 = 1111a \\ &\text{If } 1111a = 11110, \text{ then } a = 0, b = *, c = *, d = *, e = * \\ &\text{Therefore } X = 0***** \end{aligned} $	4. 0*****
<p>5. LISP</p> $ \begin{aligned} &(\text{CDR} (\text{CAR} (\text{REVERSE} (\text{CDR} '((2 (a 3) b) c (d 4 5) (e (f 6) g)))))) \\ &= (\text{CDR} (\text{CAR} (\text{REVERSE} '(c (d 4 5) (e (f 6) g)))))) \\ &= (\text{CDR} (\text{CAR} '((e (f 6) g) (d 4 5) c))) \\ &= (\text{CDR} '(e (f 6) g)) \\ &= ((f 6) g) \end{aligned} $	5. ((f 6) g)

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American Computer Science League

Contest #2

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